

## EDA ad hoc B program

# CORASMA project COgnitive RAdio for dynamic Spectrum MAnagement Contract N° B-781-IAP4-GC

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## Learning algorithms for power and frequency allocation in clustered ad hoc networks

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June 25, 2013

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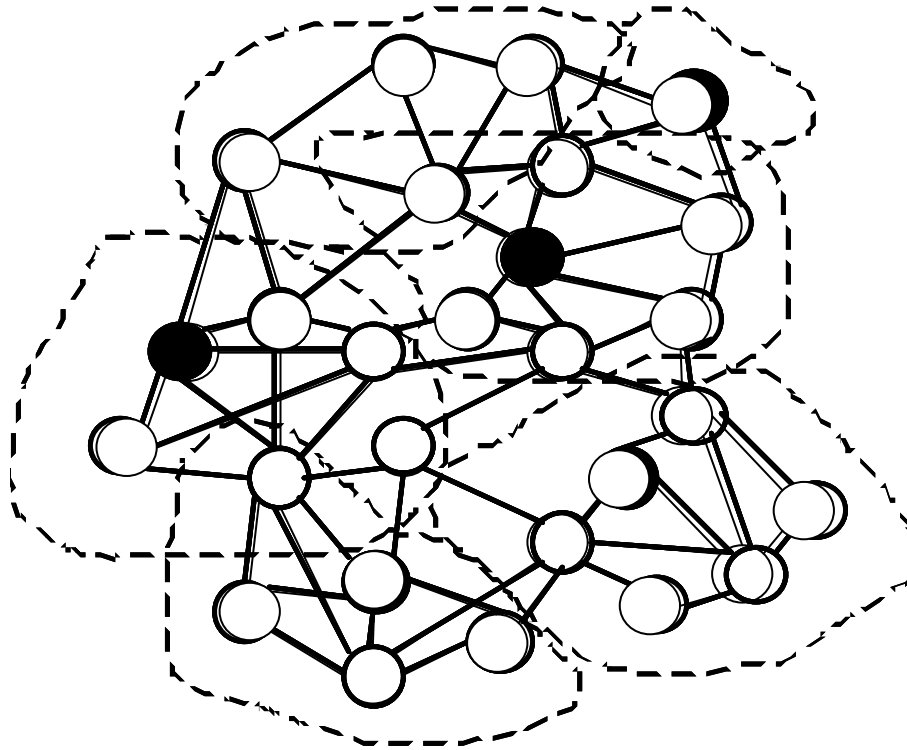
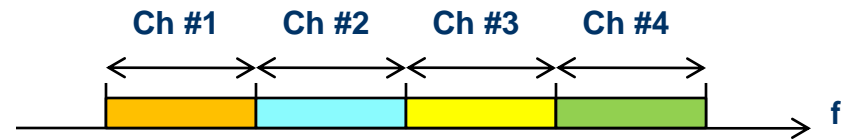
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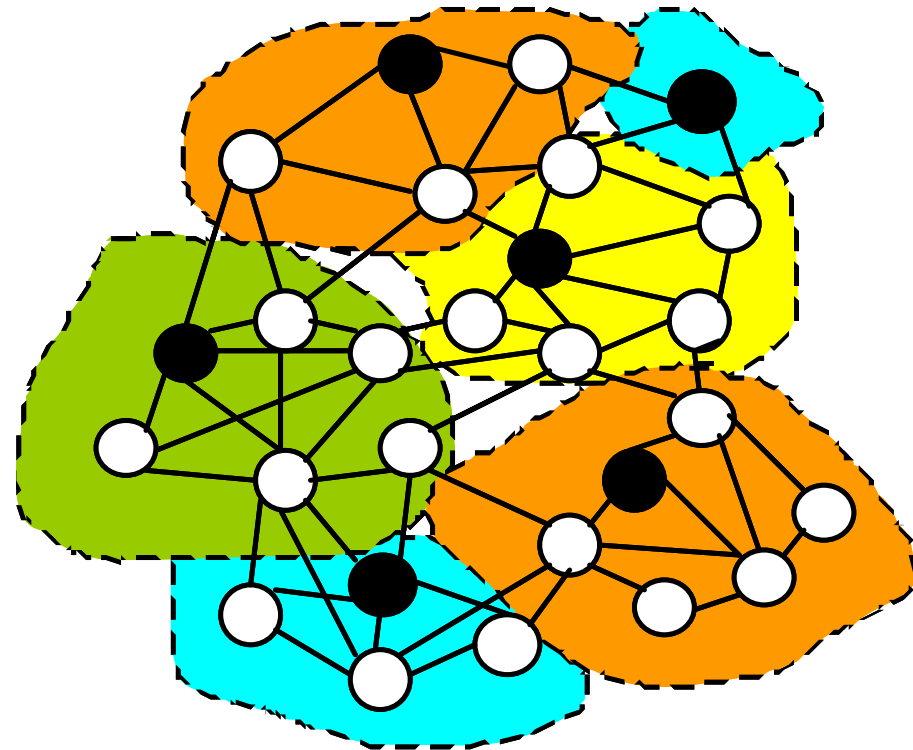
# Overview: The problem



Cluster Head



Flat network  
Clustering



Cluster frequency « coloring »

# Overview: The problem

- Optimization problem
  - Select the cluster frequency channel
    - That minimizes the total transmit power (all the clusters)
    - Subject to per-link SINR constraints
    - In a fully distributed way
  
- Several possible solutions
  - Multi-channels
    - Iterative Water-Filling
  - Single channel
    - GADIA
  - Game Theory-based
    - Reinforcement Learning
    - Trial and Error

- Iterative Water-filling
  - Individually optimum
  - No proof of convergence
  - Several results show its inefficiency in densely populated networks (Tragedy of the Commons)
- GADIA
  - Channel selected to minimize the global interference level
  - Convergence proved
  - Not adapt to set power and channel, requires distanced clusters
- Reinforcement Learning
  - Convergence proved
  - Slow convergence
  - Different training and exploitation periods

# Trial and Error: basic strategy

## Trial and Error Learning

(H. Peyton Young, 2009)

### Moods

c: content

d: discontent

w: watchful

h: hopeful

### - Content

. Experiments new actions with probability  $\varepsilon$

### - Discontent

. Experiments new actions

### - C -> H: no experiment, utility increases

. H -> C: if utility increases or equal

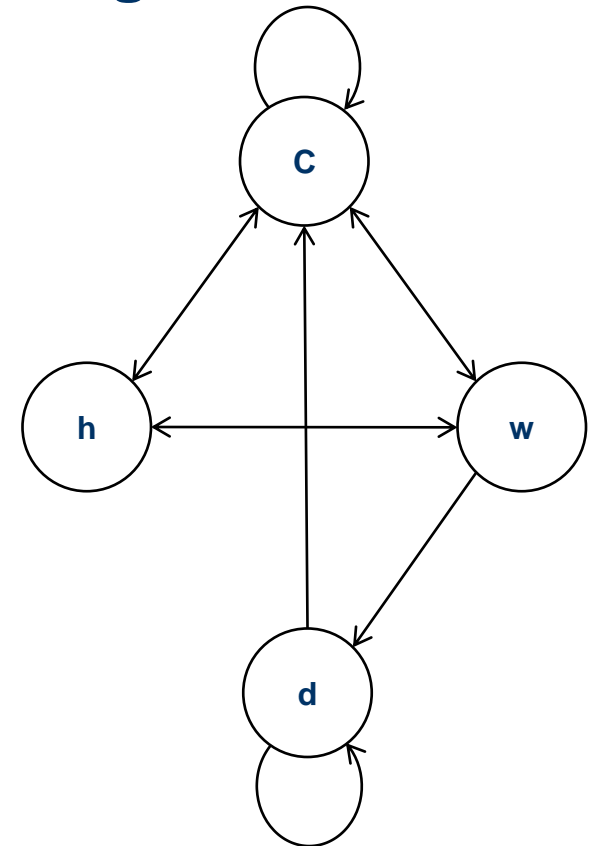
. H -> W: if utility decreases

### - C -> W: no experiment, utility decreases

. W -> H: if utility increases

. W -> C: if utility equal

. W -> D: if utility decreases

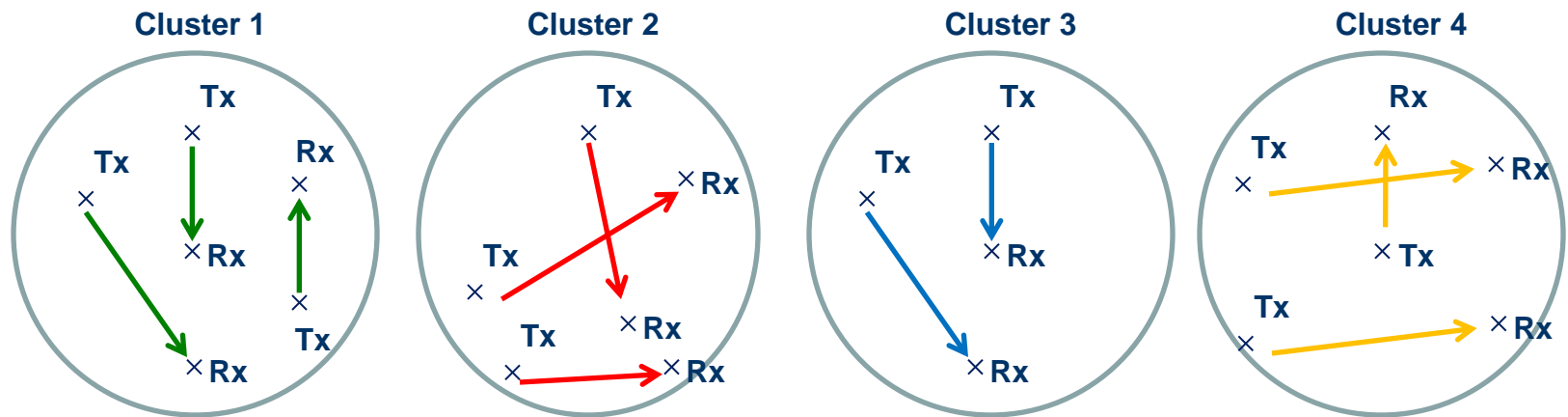


# From original TE to ad hoc networks...

## First step



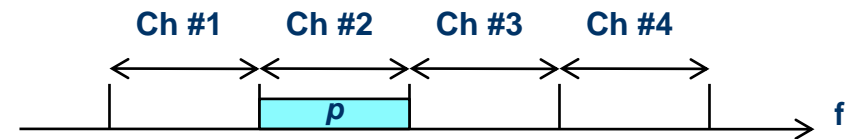
## To



# Trial and Error: Utility function

## Proposed solution: Trial and Error algorithm

- Players: CHs
- Actions: powers/frequencies
- Utility for CH #k:



$$u_k(\mathbf{p}) := \frac{1}{1 + |L_k| \beta} \left( \underbrace{1 - \frac{p_k}{p_{MAX}}}_{\text{Power minimization}} + \underbrace{\beta \sum_{\ell \in L_k} 1_{[\Gamma_\ell(\mathbf{p}) > \Gamma_k]}}_{\text{SINR constraints}} \right)$$

# Trial and Error: Theoretical Results

## ■ Theorem

- For  $\Gamma$ , if  $\mathbf{a}^*$  is a solution of the optimization problem and  $\mathbf{a}^*$  is a NE, then TE converges to  $\mathbf{a}^*$

## ■ Theorem

- For  $\Gamma$ , the TE converges to the NE where the largest set of nodes are simultaneously satisfied

## ■ Property

- TE selects among all the NE the one maximizing the Social Welfare



# Trial and Error: some issues

## ■ Issues

- Instability of the solution even if optimal
  - One parameter decides the experimentation frequency on both channels and power levels
  - Parameter fixed a priori
- Slow convergence
- Experimentation do not take “common sense” behavior

# Enhanced Trial and Error

- Solution: enhanced Trial and Error (ETE)
  - Two different experimentation frequency
    - sets the experimentation frequency on the power levels
    - sets the experimentation frequency on the channels
    - is time-varying:

$$\varepsilon_c(t) = \begin{cases} \max\left(\frac{\varepsilon_c(t-1)}{2}, \varepsilon_{\min}\right) & \text{if } \sum_{\ell \in L_k} 1_{[\Gamma_\ell(\mathbf{p}) > \Gamma_k]} = |L_k| \\ \varepsilon_c(0) & \text{otherwise} \end{cases}$$

- “Small” makes the channel-cluster association scheme stable

# Enhanced Trial and Error

## ■ Solution: enhanced Trial and Error (ETE)

### ■ Smart probability distribution for power experimentation

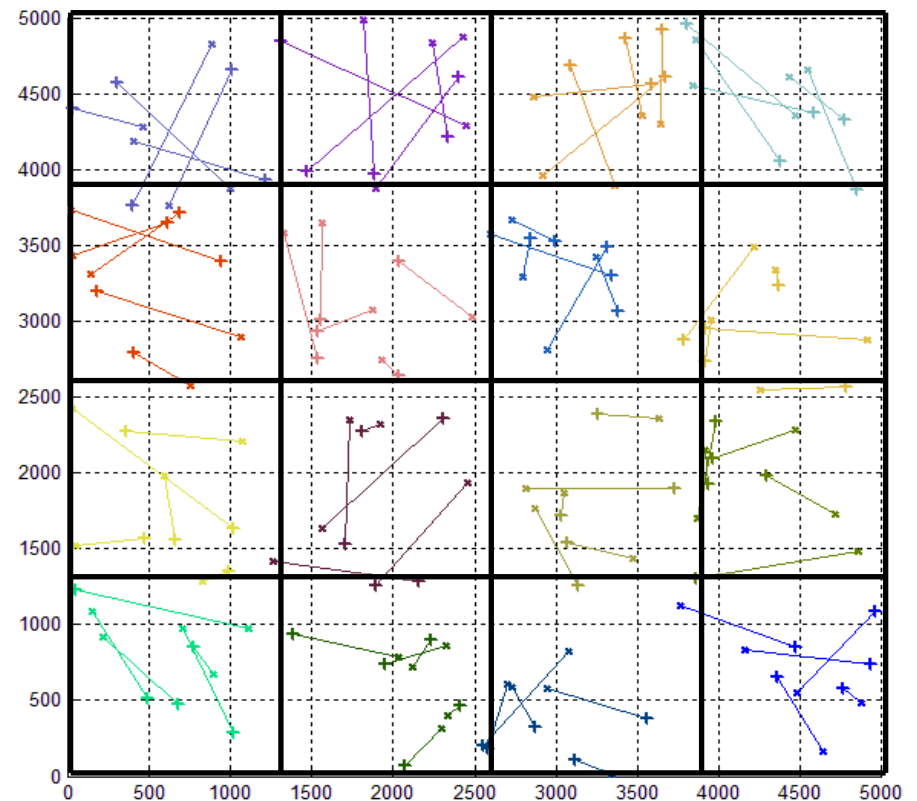
■ Content and  $\sum_{\ell \in L_k} 1_{[\Gamma_\ell(\mathbf{p}) > \Gamma_k]} = |L_k|$ : experiment only levels below

■ Content and  $\sum_{\ell \in L_k} 1_{[\Gamma_\ell(\mathbf{p}) > \Gamma_k]} < |L_k|$ : experiment all levels

■ Discontent: 
$$p_k = \begin{cases} p_{\text{MAX}} & \text{with prob. } \min\left(\frac{C}{K}, 1\right) \\ 0 & \text{with prob. } \max\left(1 - \frac{C}{K}, 0\right) \end{cases}$$

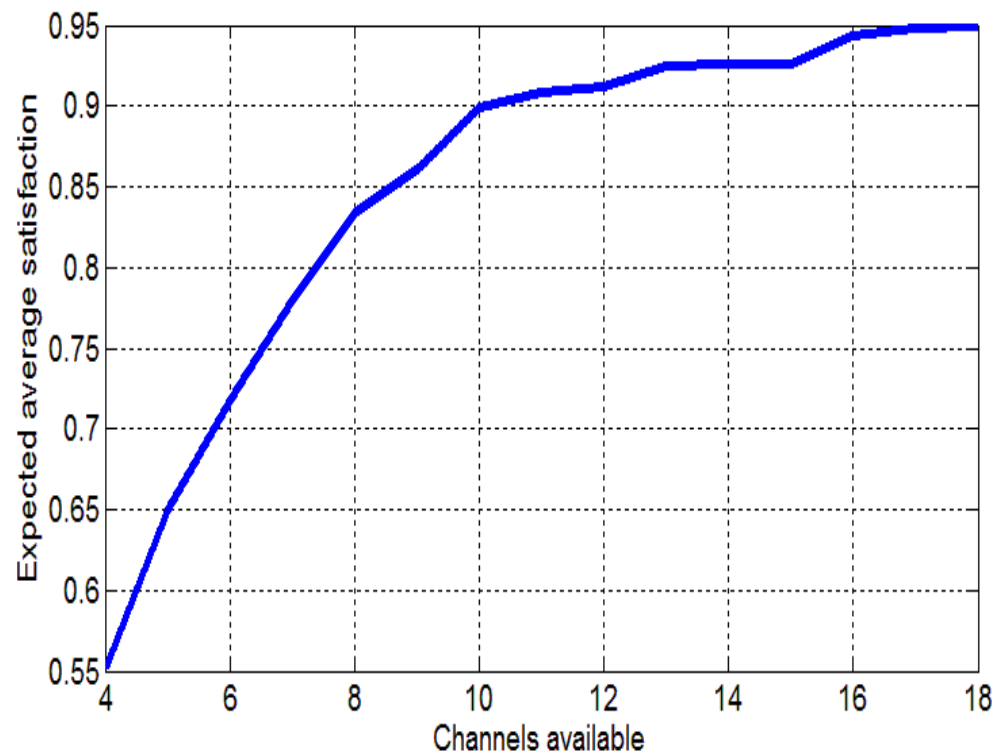
# Numerical Simulations

- Static dense scenario
  - Nodes fixed in a square area
  - 16 “square” clusters
  - 4 links per cluster
  - Channel-range: 2-18
  - Block fading channels
  - Rayleigh fading channels



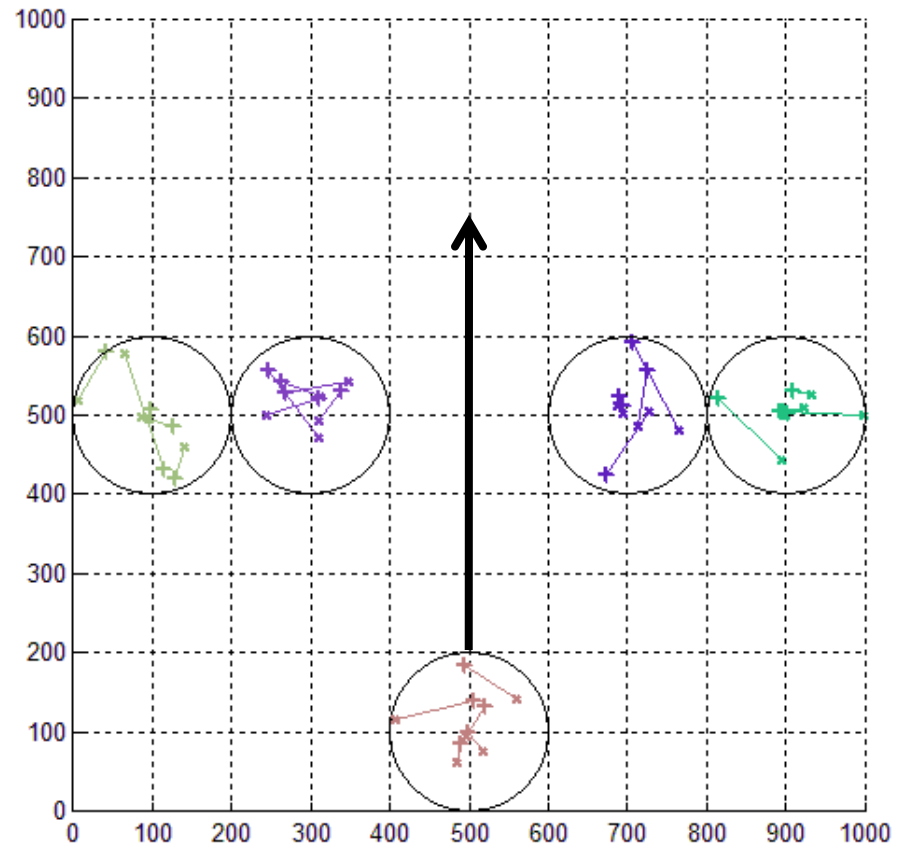
# Simulation results

## ■ Dense scenario



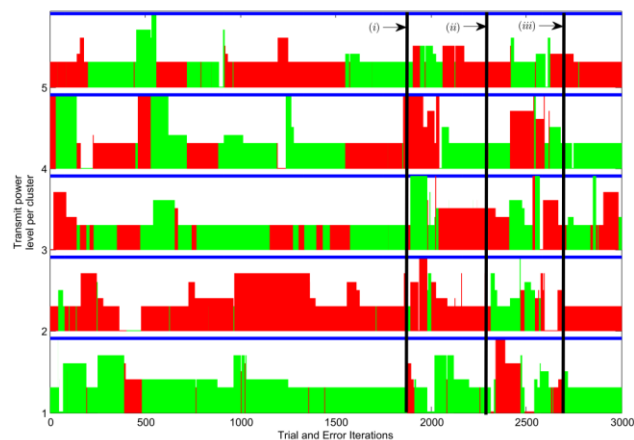
# Numerical Simulations

- Mobility scenario
  - 4 clusters fixed
  - 1 moving cluster
  - 2 frequency channels

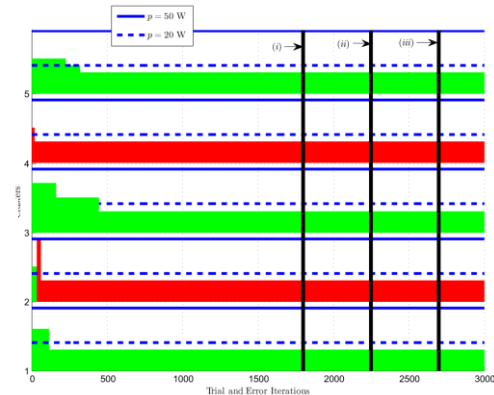
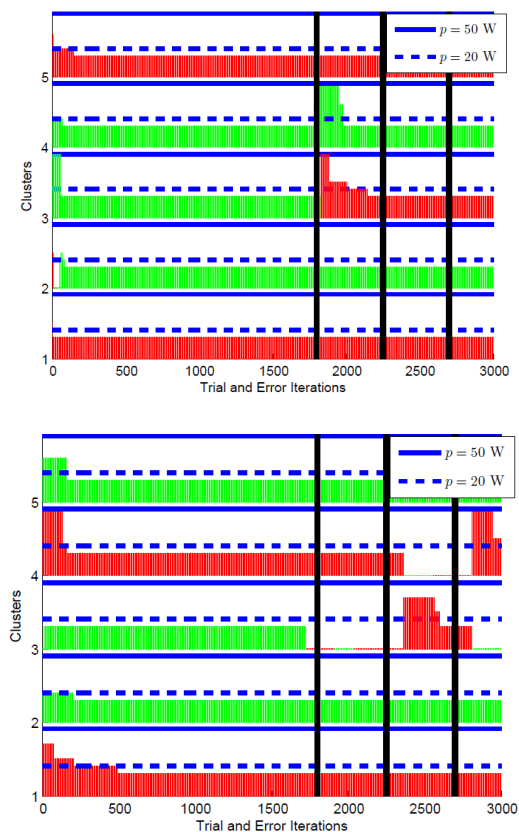


# Channels and power levels – Mobility scenario

Standard TE



Enhanced TE



# Enhanced Trial and Error - Conclusions

- Sets efficiently channel and power levels
  - Requires only intra-cluster information
  - Quickly adapts to changes in the network topology
  - Quickly adapts to fading
- 
- Thus looks adapted from a theoretical point of view
  - And validated by simulations

## **Using Matlab simulations!**

- Next challenge: make it work into a real system
- Ongoing implementation in a HiFi network simulator...